

Conversion from Packet Error Rate (PER) to Bit Error Rate (BER) by modelling CCK bit errors.

The 11 Mbps CCK implementation encodes a byte stream using 2^8 different out of 2^{16} symbols of 8 chips each.

Notations:

PER = Packet Error Rate
BER = Bit Error Rate
SER = Symbol Error Rate
N = Packet length in bytes
NS = Packet length in symbols

Assumptions:

1. An erroneously interpreted symbol will produce any of the other symbols with equal probability.
2. Symbol errors are considered to be independent of each other.
3. The 1 Mbps preamble and header are not CCK encoded and are assumed error-free. They are ignored in the discussion below.
4. One byte corresponds to one symbol exactly: NS=N.

From assumption 1 it follows that one erroneous symbol on average contains: $(8 * 128)/(256-1) = 4.016$ erroneous bits. From this it follows that:

$$(a) \quad \text{BER} = \text{SER} * (4.016/8 \text{ chips}) = \text{SER} * 0.502$$

From assumption 2 the rate of errorless packets (1-PER) depends on the rate of errorless symbols (1-SER) in the following way:

$$(b) \quad (1-\text{PER}) = (1-\text{SER})^{\text{NS}}$$

or, using (a) and assumption 4:

$$(c) \quad \text{PER} = 1 - (1 - (1.992 * \text{BER}))^N$$

For a BER of 1E-5 (as required for FCC approval), and a packet size of a 1000 bytes, this leads to a PER of 0.02 (which is 2%).

A PER of 8% corresponds with a BER of 4.2E-5.